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13 **Diagnosis of a North American Polar/Subtropical Jet Superposition Employing Piecewise**
14 **Potential Vorticity Inversion**
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[1] Throughout this study, tropopause specifically refers to the dynamic tropopause, which is defined as a surface of

**Abstract**

The polar jet (PJ) and subtropical jet (STJ) often reside in different climatological latitude bands. On occasion, the meridional separation between the two jets can vanish, resulting in a relatively rare vertical superposition of the PJ and STJ. A large-scale environment conducive to jet superposition can be conceptualized as one that facilitates the simultaneous advection of tropopause-level potential vorticity (PV) perturbations along the polar and subtropical waveguides towards middle latitudes. Once these PV perturbations are transported into close proximity to one another, interactions between tropopause-level, lower-tropospheric, and diabatically-generated PV perturbations work to restructure the tropopause into the two-step, pole-to-equator tropopause structure characteristic of a jet superposition.

This study employs piecewise PV inversion to diagnose the interactions between large-scale PV perturbations throughout the development of a jet superposition during the 18–20 December 2009 Mid-Atlantic Blizzard. While the influence of PV perturbations in the lower troposphere as well as those generated via diabatic processes were notable in this case, tropopause-level PV perturbations played the most substantial role in restructuring the tropopause prior to jet superposition. A novel PV partitioning scheme is presented that isolates PV perturbations associated with the PJ and STJ, respectively. Inversion of the jet-specific PV perturbations suggests that these separate features make distinct contributions to the restructuring of the tropopause that characterizes the development of a jet superposition.

## 1. Introduction

The atmosphere typically exhibits the three-step pole-to-equator tropopause structure shown in Fig. 1a, with each break in the tropopause height associated with a jet stream[1]. The polar jet (PJ) stream resides at middle latitudes in the break between the polar (~350 hPa) and subtropical (~250 hPa) tropopauses and is situated atop the strongly baroclinic, tropospheric-deep polar front (e.g., Palmén and Newton 1948; Namias and Clapp 1949; Newton 1954; Palmén and Newton 1969; Keyser and Shapiro 1986; Shapiro and Keyser 1990). The subtropical jet (STJ) stream is located equatorward of the PJ (~30°N in the Northern Hemisphere) in the break between the subtropical tropopause and the even higher tropical tropopause (~100 hPa) and is characterized by modest baroclinicity in the upper troposphere and lower stratosphere (e.g., Loewe and Radok 1950; Yeh 1950; Koteswaram 1953; Mohri 1953; Koteswaram and Parthasarathy 1954; Sutcliffe and Bannon 1954; Krishnamurti 1961; Riehl 1962).

While the separate polar and subtropical jets typically reside in different climatological latitude bands, their meridional separation occasionally vanishes, resulting in a relatively rare vertical superposition of the PJ and STJ (Christenson 2013). A vertical cross section through a jet superposition is shown in Fig. 1b, which highlights three of the primary attributes of a superposition: (1) the development of a two-step tropopause structure from polar to tropical latitudes, rather than the more common three-step structure shown in Fig. 1a, (2) a consolidation of the upper-tropospheric and lower-stratospheric baroclinicity associated with each jet into substantially narrower zones of contrast, and (3) anomalously strong wind speeds associated with the aforementioned increase in baroclinicity.

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[1] Throughout this study, tropopause specifically refers to the dynamic tropopause, which is defined as a surface of constant potential vorticity (e.g., Morgan and Nielsen-Gammon 1998). In line with previous work, we select the 2-PVU surface (1 PVU = $10^{-6}$ K m$^2$ kg$^{-1}$ s$^{-1}$). The term, jet, will also be synonymous with jet streak in the text and refers to a zonally confined wind speed maximum along either the polar or subtropical waveguide.

94    The observations of the tropopause discussed with reference to Fig. 1 served as the

95    foundation for the objective identification scheme for the PJ, STJ, and superposed jets outlined in

96    Winters and Martin (2014). Employing that jet identification scheme as part of an analysis of the

97    historic 1–3 May 2010 Nashville Flood, Winters and Martin (2014) determined that the

98    development of a jet superposition was a critical component in the evolution of that flooding

99    event. A cursory reexamination of a number of other historical and recent high-impact weather

100   events over North America and the North Atlantic by the authors suggests that superposed jets

101   were a component of their evolution, as well (e.g., Defant 1959; Hoskins and Berrisford 1988;

102   Hakim et al. 1995, 1996; Bosart et al. 1996; Christenson 2013).

103   The association of jet superpositions with a class of high-impact weather events

104   motivated Winters and Martin (2016, hereafter WM16) to diagnose the development of a jet

105   superposition in two cases: the 18–20 December 2009 Mid-Atlantic Blizzard and the

106   aforementioned 1–3 May 2010 Nashville Flood. These cases demonstrated that elements of both

107   the antecedent remote and local synoptic environments are important to consider when

108   diagnosing the development of a superposition. A large-scale environment conducive to jet

109   superposition is broadly conceptualized in Fig. 2 as one that facilitates the simultaneous

110   advection of tropopause-level cyclonic and anticyclonic potential vorticity (PV) perturbations

111   from polar and tropical latitudes, respectively, and the subsequent horizontal juxtaposition of

112   those PV perturbations at middle latitudes.

113   Much attention in the literature has focused on the origin and characteristics of these

114   tropopause-level PV perturbations. Polar cyclonic PV perturbations, which have been referred to

115   as coherent tropopause disturbances (CTDs; Pyle et al. 2004), are typically located along the

116   polar waveguide, accompanied by a PJ on their equatorward flank (Fig. 2), and exhibit a

117  localized depression in the height of the tropopause. One particular class of CTD that has

118  received specific attention is the tropopause polar vortex (TPV), which primarily forms as a

119  result of an enhanced vertical gradient in radiative heating near the tropopause at polar latitudes

120  (Cavallo and Hakim 2010). As CTDs are transported towards middle latitudes by the background

121  flow within which they are embedded, they occasionally initiate surface cyclogenesis (e.g.,

122  Hakim et al. 1995, 1996; Pyle et al. 2004; Cavallo and Hakim 2010).

123      In contrast to polar latitudes, where polar cyclonic PV perturbations are manifest on the

124  tropopause as coherent vortices, tropical anticyclonic PV perturbations are not readily

125  identifiable on the tropopause at tropical latitudes (i.e., Morgan and Nielsen-Gammon 1998, their

126  Fig. 2). Instead, the tropical upper-troposphere is characterized by a reservoir of uniform, low PV

127  air that is continuously replenished by mass deposition in the upper troposphere from tropical

128  convection. Once this tropical, low PV air is transported poleward via tropical plumes or the

129  presence of a low-latitude trough (e.g., Liebmann and Hartmann 1984; Iskenderian 1995;

130  Roundy et al. 2010; Fröhlich et al. 2013; Archambault et al. 2013, 2015; WM16), it becomes

131  manifest as an anticyclonic PV perturbation along the subtropical waveguide with a STJ

132  positioned on its poleward flank (Fig. 2). Not only are these tropical anticyclonic PV

133  perturbations accompanied by an upper-tropospheric thermodynamic environment characterized

134  by weak static stability, but also by the occasional presence of atmospheric rivers (Newell et al.

135  1992; Zhu and Newell 1998; Ralph et al. 2004) within the poleward-directed branch of their

136  anticyclonic circulation. Consequently, the horizontal juxtaposition of polar cyclonic and tropical

137  anticyclonic PV perturbations at middle latitudes typifies a dynamical and thermodynamic

138  environment conducive to the production of high-impact weather.

139    As polar cyclonic and tropical anticyclonic PV perturbations are transported into close

140    proximity to one another, the individual non-divergent circulations associated with each PV

141    perturbation add constructively to produce the anomalously strong upper-tropospheric wind

142    speeds associated with a superposed jet. In addition, mesoscale processes within the near-jet

143    environment, such as ageostrophic transverse circulations and proximate midlatitude convection

144    (Fig. 2), can act to locally restructure the tropopause into the two-step structure characteristic of

145    a jet superposition (WM16). While WM16 note the relevance of dynamical structures within the

146    remote synoptic environment to the production of a superposition, stronger emphasis is placed on

147    the role of mesoscale processes within the near-jet environment. Consequently, a detailed

148    understanding of the large-scale interaction between tropopause-level PV perturbations along the

149    polar and subtropical waveguides during a jet superposition event remains unresolved.

150    A particularly effective way to examine the large-scale interaction between separate PV

151    perturbations during the development of a jet superposition is to employ piecewise PV inversion,

152    which leverages the intrinsic principles of PV conservation and invertibility (e.g., Hoskins et al.

153    1985; Thorpe 1985; Robinson 1988; Holopainen and Kaurola 1991; Davis and Emanuel 1991).

154    Specifically, these principles imply that (1) the PV serves as a particularly good tracer for

155    atmospheric motion under the assumption of adiabatic and inviscid flow and (2) knowledge of a

156    PV perturbation at a particular time, along with a suitable balance condition, permits a recovery

157    of the mass and thermal fields associated with that PV perturbation.

158    Piecewise PV inversion has been employed extensively to examine a number of different

159    tropospheric processes. In particular, piecewise PV inversion has fostered insight into surface

160    cyclogenesis (e.g., Davis and Emanuel 1991; Davis 1992a,b; Davis et al. 1993; Davis et al. 1996;

161    Nielsen-Gammon and Lefevre 1996; Morgan and Nielsen-Gammon 1998), midlatitude trough

162  interaction (e.g., Hakim et al. 1996), tropospheric frontogenesis (e.g., Morgan 1999; Korner and

163  Martin 2000), the development and movement of tropical cyclones (e.g., Wu and Emanuel

164  1995a,b; Shapiro 1996; Shapiro and Franklin 1999; McTaggart-Cowan et al. 2001; Shapiro and

165  Möller 2003), and understanding of tropical–extratropical interactions (e.g., McTaggart-Cowan

166  et al. 2001, 2004, Agustí-Panareda et al. 2004; Ahmadi-Givi et al. 2004; Grams et al. 2011,

167  2013).

168      The analysis performed by Wandishin et al. (2000), however, is of particular relevance

169  when considering the application of PV inversion to diagnose the development of a jet

170  superposition. In that study, piecewise quasi-geostrophic (QG) PV inversion was employed to

171  examine the development of an idealized tropopause break. The analysis determined that vertical

172  motion at the tropopause initiated the development of a tropopause break by vertically tilting an

173  initially flat portion of the tropopause. Once the tropopause exhibited a vertical slope, the

174  presence of a vertical shear acted to further tilt the tropopause in the vertical, completing the

175  production of the tropopause break (Wandishin et al. 2000; their Fig. 4).

176      For the present work, which centers on diagnosing the vertical alignment of two distinct

177  tropopause breaks, both differential horizontal displacement and vertical motion are likely to

178  play important roles. As an idealized example, Fig. 3 depicts a vertical wind profile (red arrows)

179  that would result in a poleward displacement of the subtropical tropopause break and an

180  equatorward displacement of the polar tropopause break. This differential horizontal

181  displacement of the two tropopause breaks may promote their vertical alignment at a later time.

182  In addition, vertical motion (blue arrow) positioned between the polar and subtropical tropopause

183  breaks has the capability to alter the elevation of the subtropical tropopause and contribute to the

184  production of the two-step tropopause structure characteristic of a jet superposition (WM16).

185    While the nature of the interaction between tropopause-level PV perturbations along the

186    polar and subtropical waveguides, and their role in the production of a jet superposition, is of

187    particular interest to this study, it is also apparent that jet superposition events can be associated

188    with surface cyclogenesis and midlatitude convection (WM16). Consequently, a holistic

189    understanding of the process of jet superposition from a PV perspective necessitates

190    consideration of the influence that both lower-tropospheric and diabatically-generated PV

191    perturbations have on the production of a jet superposition, as well. With this in mind, the

192    forthcoming analysis isolates tropopause-level, lower-tropospheric, and diabatically-generated

193    PV perturbations during a well-established case of jet superposition analyzed by WM16. These

194    PV perturbations are subsequently inverted in an effort to diagnose the dynamical structures that

195    contribute the most towards restructuring the tropopause during a jet superposition event.

196    The remainder of this study is structured as follows. Section 2 discusses the methodology

197    employed in this study to partition the PV distribution and to perform piecewise PV inversion.

198    Section 3 applies piecewise PV inversion to a well-established case of jet superposition

199    previously examined by WM16 and Section 4 finishes with a brief discussion and some

200    conclusions.

201    **2. Methodology**

202    This study considers the development of a jet superposition during the 18–20 December

203    2009 Mid-Atlantic Blizzard, which was chosen to complement the analysis previously performed

204    on this case by WM16. For more specific information on the impacts of this case, the reader is

205    referred to WM16. Wind, temperature, geopotential height, and relative humidity data for this

206    case was acquired from National Centers for Environmental Prediction (NCEP) Global Forecast

207    System (GFS) analyses at 6-h intervals during the 6-day period, 0000 UTC 17 December 2009 –

208    0000 UTC 23 December 2009. The model data has a horizontal grid spacing of $1.0° \times 1.0°$ and

209    20 vertical levels, with a vertical grid spacing of 50 hPa between 1000–50-hPa. The GFS model

210    data served as boundary conditions for performing the piecewise PV inversion. The details of the

211    inversion techniques are provided in the discussion that follows.

212    *a) PV Partitioning Scheme*

213    The degree to which insight is gained from piecewise PV inversion is highly dependent

214    upon the scheme used to partition the PV distribution. Consequently, care must be taken to

215    partition the flow into a finite number of pieces, such that each piece captures a subset of the PV

216    distribution that is associated with a particular dynamical structure. The Perturbation PV (PPV)

217    at 6-h intervals was defined as the instantaneous deviation of the full PV at a grid point from the

218    6-day Mean PV (MPV) at that same grid point. The PPV was further partitioned at each 6-h

219    interval using a slightly modified version of the three-way partition described by Korner and

220    Martin (2000).

221    A conceptual diagram illustrating this three-way partition is shown in Fig. 4a. The

222    Surface PV (SPV) isolates the PPV at grid points in the 950–850-hPa isobaric layer with a

223    relative humidity < 70%, as well as all potential temperature perturbations (calculated against a

224    6-day mean for each grid point) on the bottom boundary of the domain. The SPV is designed to

225    capture the impact of near-surface temperature perturbations that behave as PV perturbations

226    along the bottom boundary of the domain (Bretherton 1966). The Interior PV (IPV) isolates the

227    PPV at grid points in the 950–150-hPa isobaric layer with a relative humidity $\geq 70\%$[2]. The IPV is

228    designed to separate the diabatic creation and destruction of PV that accompanies latent heat

229    release. Finally, the Upper-Tropospheric PV (UTPV) captures the PPV at grid points in the 650–

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[2] The relative humidity criterion is identical to that used by Davis (1992b) and Korner and Martin (2000). In those studies, this threshold was chosen to capture PV perturbations associated with latent heat release that may have been advected out of a region of saturated ascent and into a region of weak subsidence (e.g., subsaturated air).

230    100-hPa isobaric layer with a relative humidity < 70%, as well as all temperature perturbations

231    on the top boundary of the domain. The UTPV isolates dry air of either stratospheric or upper-

232    tropospheric origin and captures the PPV tied to dynamical structures in the middle and upper

233    troposphere, including the PJ and STJ. Together, the SPV, IPV, and UTPV account for nearly all

234    of the PPV within the domain, except for dry air between 800–700-hPa and nearly saturated air

235    above 150-hPa. An examination of this residual PPV demonstrates that it is negligible and its

236    omission does not significantly impact the analysis.

237          While a three-way partition of the PPV provides insight into the interaction between PV

238    perturbations in the lower and upper troposphere and those generated via diabatic processes, it

239    does not separate the influence of individual PV perturbations along the polar and subtropical

240    waveguides during a jet superposition event (i.e., polar cyclonic and tropical anticyclonic PV

241    perturbations). Consequently, an additional partitioning scheme is employed to isolate the PPV

242    associated with the PJ and STJ, respectively. In the upper troposphere and lower stratosphere, an

243    individual tropopause break is characterized in Fig. 4b by the horizontal juxtaposition of a

244    positive PV perturbation on the poleward side of the tropopause break and a negative PV

245    perturbation on the equatorward side of the tropopause break (e.g., Davies and Rossa 1998;

246    Morgan and Nielsen-Gammon 1998; Pyle et al. 2004). The non-divergent circulations

247    accompanying these PV perturbations subsequently combine to drive a jet that is situated parallel

248    to its respective tropopause break. To capture these PV perturbations, the partitioning scheme

249    isolates the PPV associated with each jet by considering the characteristic isentropic layers that

250    contain the polar and subtropical tropopause breaks.

251          The isentropic layers used for the jet PV partition are subjective and are heavily

252    dependent upon the case under consideration. For the 18–20 December 2009 Blizzard, the Polar

253    Jet PV (PJPV) isolates the PPV at grid points in the 305–325-K isentropic layer with a relative

254    humidity < 70%. The implementation of a relative humidity criterion in this partition is designed

255    to remove the influence of proximate latent heat release when determining the flow associated

256    with the PJ and STJ. The Subtropical Jet PV (STJPV) isolates the PPV at grid points in the 325–

257    355-K isentropic layer with a relative humidity < 70%. An examination of potential temperature

258    on the dynamic tropopause over North America throughout the duration of this case

259    demonstrates that the 325-K isentrope routinely intersected the subtropical tropopause step (e.g.,

260    Fig. 4b). Consequently, the 325-K surface served as a suitable isentrope to differentiate between

261    the PJPV and STJPV.

262        The distribution of PJPV and STJPV within the cross section, A–A', at 0000 UTC 19

263    December 2009 is shown in Fig. 4c. An examination of the non-divergent wind associated with

264    the jet-specific PV perturbations further demonstrates that the PJPV and STJPV account for a

265    large majority of the perturbation flow associated with the PJ and STJ, respectively (not shown).

266    While the PJPV and STJPV are not a strict partition of the UTPV, their sum closely

267    approximates the distribution and magnitude of the UTPV. Consequently, an examination of the

268    three-dimensional circulations associated with the PJPV and STJPV provides insight into the

269    nature of the interaction between PV perturbations along the polar and subtropical waveguides

270    during the development of a jet superposition.

271    *b) Piecewise PV Inversion Techniques*

272        Since substantial flow curvature and diabatic processes routinely characterize jet

273    superposition events (WM16), an inversion of the Ertel PV (Ertel 1942) is more suitable for

274    diagnosing the interaction between PV perturbations during a jet superposition event than QGPV

275    inversion. For the present study, a static PV inversion was used to invert the Ertel PV for its

276   associated geopotential, $\phi$, and non-divergent streamfunction, $\psi$. The methodology for

277   performing the static PV inversion is identical to that described by Davis and Emanuel (1991)

278   and the reader is encouraged to consult that work for any technical details.

279        Full and piecewise static PV inversions were performed within a North American domain

280   bounded horizontally from 130°W–50°W and 10°N–65°N and vertically by the 1000-hPa and

281   50-hPa isobaric surfaces. For an inversion of the full PV, the analyzed geopotential height from

282   the GFS was used to prescribe $\phi$ on the lateral boundaries as a Dirichlet boundary condition. The

283   boundary $\psi$ was specified using a Neumann boundary condition such that (1) the component of

284   the wind from the GFS analysis perpendicular to the boundary was equivalent to the gradient of

285   $\psi$ along the boundary and (2) by ensuring that there was no net divergence out of the domain.

286   Hydrostatic balance and the vertically averaged potential temperature, $\theta$, between 1000–950 hPa

287   (100–50 hPa) were used to define a Neumann boundary condition for $\phi$ and $\psi$ on the bottom

288   (top) boundary of the domain. In order to converge on a solution for $\phi$ and $\psi$, negative values of

289   PV were changed to a small positive constant (0.01 PVU; 1 PVU = $10^{-6}$ K m$^2$ kg$^{-1}$ s$^{-1}$) and the

290   static stability was not permitted to become negative.

291        The methodology for inverting the MPV is identical to the full PV, but with the $\phi$, $\psi$, and

292   $\theta$ fields from the GFS analysis replaced by a 6-day average of those variables, $\bar{\phi}$, $\bar{\psi}$, and $\bar{\theta}$, along

293   the boundaries using a Dirichlet boundary condition. Lateral and horizontal Dirichlet boundary

294   conditions for an inversion of the full PPV, $\phi'$, $\psi'$, and $\theta'$, were specified as the difference

295   between the boundary $\phi$, $\psi$, and $\theta$ from the full PV inversion and the MPV inversion (i.e., $\phi -$

296   $\bar{\phi} = \phi'$). Lateral Dirichlet boundary conditions, with $\phi' = 0$ and $\psi' = 0$, were established for

297   inversions of the SPV, IPV, UTPV, PJPV, and STJPV, while $\theta'$ at the top and bottom boundaries

298    for these inversions was specified using a Dirichlet boundary condition according to the

299    partitioning scheme discussed in Section 2a.

300        A static PV inversion only returns the balanced, non-divergent flow associated with each

301    subset of the PV distribution. Given that vertical motion can also play a substantial role in

302    restructuring the tropopause during a jet superposition event (WM16), recovery of the balanced

303    divergent flow associated with each subset of the PV distribution was also required. This

304    particular task was accomplished by inverting the system of prognostic balance equations

305    described in Davis and Emanuel (1991). This technique returned the geopotential tendency, $\phi^t$,

306    streamfunction tendency, $\psi^t$, PV tendency, $q^t$, velocity potential, $\chi$, and vertical motion, $\omega$,

307    associated with each subset of the PV distribution.

308        Convergence on a solution to the system of prognostic balance equations for this case

309    required using Dirichlet boundary conditions to set the lateral boundaries of $\phi^t$, $\psi^t$, $q^t$, $\chi$, and $\omega$

310    equal to zero, as well as the top and bottom boundaries of $q^t$, $\chi$, and $\omega$ equal to zero. $\phi^t$ and $\psi^t$

311    along the top and bottom boundaries were determined using a Neumann boundary condition by

312    calculating the time tendency of the hydrostatic equation and the potential temperature tendency,

313    $\theta^t$. The latent heating term ($d\theta/dt$) in the system of prognostic balance equations was calculated

314    following the method employed in Emanuel et al. (1987) and Winters and Martin (2014). In

315    order to converge consistently on a solution to the system of prognostic balance equations,

316    smoothing of the individual forcing terms in the $\omega$-equation was required. As for the static PV

317    inversion, the reader is referred to Davis and Emanuel (1991) for more specific information on

318    the system of prognostic balance equations and its inversion.

319        The combination of the static and prognostic PV inversion recovers the balanced three-

320    dimensional flow associated with each subset of the PV distribution. The unbalanced portion of

321    the flow cannot be returned via these methods and falls into a residual term, which primarily

322    corresponds to the non-divergent component of the ageostrophic wind (e.g., Davis et al. 1996).

323    For the case considered in this study, the unbalanced portion of the flow exceeded 20 m s$^{-1}$ in the

324    immediate vicinity of the developing superposed jet core[3] and was aligned anti-parallel to, and

325    was considerably weaker than, the balanced non-divergent wind (not shown). Consequently, the

326    restructuring of the tropopause accomplished by the unbalanced portion of the flow was greatly

327    overshadowed by that of the balanced flow at all times considered. As a result, the process of

328    superposition, insofar as it depends on rearrangement of the tropopause, was well explained by

329    the balanced portion of the flow.

330    **3.  Jet Superposition during the 18–20 December 2009 Mid-Atlantic Blizzard**

331    *a) Case Overview*

332    The overview that follows mirrors that provided by WM16 and it is reproduced here

333    because of its relevance to the present study. At 0000 UTC 19 December, a confluent flow

334    pattern was situated over the eastern United States at 250 hPa with a PJ (dashed blue line)

335    located[4] in northwesterly flow over the Central Plains and a STJ (red dashed line) extending

336    from Mexico northeastward over the Gulf of Mexico (Fig. 5a). The surface cyclone responsible

337    for producing blizzard conditions across the Mid-Atlantic States was characterized by a

338    minimum sea-level pressure below 1000 hPa and was positioned in a favorable location for

339    continued development beneath the left exit region of the STJ. A vertical cross section through

340    the PJ and STJ highlights the presence of a three-step tropopause structure and demonstrates that

341    the PJ and STJ were clearly distinct structures at this time (Fig. 1a).

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[3] Similar to this case, Davis et al. (1996) also noted that the unbalanced winds were maximized on the anticyclonic shear side of an upper-level jet stream in their analysis of the ERICA-IOP-4 storm.

[4] PJ and STJ axes shown in Fig. 5 are identical to those shown in Fig. 5 of WM16. The axes were identified in WM16 by employing the objective jet identification scheme outlined in Winters and Martin (2014).

342       During the intervening 18 h, the PJ intensified and propagated downstream into the base

343    of an upper-level trough centered over the Great Lakes, such that the PJ axis was aligned parallel

344    to the STJ at 1800 UTC 19 December (Fig. 5b). The STJ also intensified during this interval and

345    shifted poleward of its previous position into the southeastern United States. A cross section

346    through both jet structures at this time demonstrates that, while the jet axes were located in closer

347    proximity to one another, a three-step tropopause structure persisted (Fig. 9b). Additionally, the

348    surface cyclone deepened ~8 hPa from the prior time beneath the left exit region of the STJ, as

349    heavy snowfall continued to impact the Mid-Atlantic States in the cyclone's northwest quadrant.

350       By 1200 UTC 20 December, the axis of the PJ shifted southeastward, as the trough over

351    the Great Lakes continued to deepen, and the STJ migrated farther poleward into the

352    southeastern United States. The combination of these displacements resulted in a vertical

353    superposition (yellow line) of the PJ and STJ from southern Georgia northeastward to off the

354    coast of North Carolina (Fig. 5c). A cross section through the superposed jet at this time

355    indicates a marked increase in jet wind speeds, intensified upper-tropospheric and lower-

356    stratospheric baroclinicity in the vicinity of the jet core, and the development of a two-step

357    tropopause structure (Fig. 1b). Beneath the left exit region of the superposed jet, the surface

358    cyclone continued to deepen rapidly off the New England coast, reaching a minimum sea-level

359    pressure below 980 hPa. The preceding discussion suggests that this case contains PV

360    perturbations associated with the PJ and STJ, as well as PV perturbations associated with the

361    surface cyclone and its extensive precipitation shield. Consequently, it is prudent to consider the

362    role played by each of these PV perturbations during the process of jet superposition.

363       For brevity, the foregoing analysis is restricted to diagnosing the displacement of the

364    tropopause at a single time, 1800 UTC 19 December, 18 h prior to superposition. The results

365    from this time were found to be representative of the entire 36-h period discussed above and

366    permit a synthesis with the previous analysis performed on this case by WM16.

367        *b) Differential Horizontal Displacement of the Tropopause Breaks*

368        As discussed with reference to Fig. 3, both a differential horizontal displacement of the

369    individual tropopause breaks and a vertical displacement of the tropopause steps can contribute

370    to the production of a superposed jet's two-step tropopause structure. To diagnose the three-

371    dimensional displacement of the tropopause, PV advection (PVA) within the domain was

372    calculated by setting all values of PV < 1.5 PVU (> 2.5 PVU) equal to 1.5 PVU (2.5 PVU). This

373    ensures that any diagnosed areas of PVA were restricted to the immediate vicinity of the 2-PVU

374    surface and implied a horizontal or vertical displacement of the tropopause. The subsequent

375    analysis examines the differential horizontal displacement of the polar and subtropical

376    tropopause breaks by calculating PVA within the 1.5–2.5-PVU channel at 300- and 200 hPa,

377    respectively. These isobaric levels are particularly suitable for diagnosing the horizontal

378    displacement of the tropopause since they persistently intersect the polar and subtropical

379    tropopause breaks throughout duration of the case (Fig. 1 and Fig. 9b).

380        The PVA within the 1.5–2.5-PVU channel accomplished along the polar (blue line) and

381    subtropical (red line) tropopause breaks by the balanced non-divergent ($\vec{V}_{nd} = k \times \nabla \psi$) and

382    divergent wind ($\vec{V}_d = \nabla \chi$) at 1800 UTC 19 December is shown in Fig. 6. From this analysis, it is

383    immediately apparent that the non-divergent wind was responsible for a large majority of the

384    PVA diagnosed along each tropopause break. In particular, the polar tropopause break outlined a

385    hook-shaped region of high PV at 300 hPa over the upper Midwest and was characterized by a

386    band of negative PVA (–PVA) by the non-divergent wind from the United States/Canadian

387    border to northern Alabama and a band of positive PVA (+PVA) from the Great Lakes to the

388    Mid-Atlantic States (Fig. 6a). With virtually no PVA provided by the divergent wind at 300 hPa

389    (Fig. 6c), the PVA patterns associated with the non-divergent wind in Fig. 6a implied a

390    downstream propagation of the PV hook at 300 hPa. Importantly, a large section of the polar

391    tropopause break that paralleled the subtropical tropopause break was not characterized by

392    substantial +PVA (Fig. 6a), indicating that the non-divergent wind did not favor a systematic

393    equatorward displacement of the polar tropopause break towards its subtropical counterpart over

394    the southeastern United States at this time.

395         At 200 hPa, the subtropical tropopause break outlined the perimeter of a low-latitude

396    trough west of Mexico and extended northeastward across the Florida peninsula (Fig. 6b).

397    Localized maxima in –PVA by the non-divergent wind characterized the subtropical tropopause

398    break off the coast of South Carolina (Fig. 6b), implying a poleward shift of the subtropical

399    tropopause break towards the polar tropopause break over the Atlantic Ocean. Consequently, this

400    diagnosed poleward movement of the subtropical tropopause break off the South Carolina coast

401    directly contributed to jet superposition 18-h later (Fig. 5c). Farther upstream, an intermittently

402    continuous band of +PVA by the non-divergent wind extended along the subtropical tropopause

403    break from the base of the low-latitude trough west of Mexico northeastward towards the Gulf

404    Coast. While a fraction of the +PVA by the non-divergent wind (Fig. 6b) was offset by a thin

405    strip of –PVA by the divergent wind over the Gulf of Mexico (Fig. 6d), the diagnosed PVA

406    patterns at this time indicated that the subtropical tropopause break would either remain

407    stationary or propagate eastward in locations over the Gulf of Mexico. Consequently, the

408    analysis at this time does not support a vertical superposition of the two tropopause breaks via

409    differential horizontal displacement in locations west of Florida.

410     Given that the non-divergent wind was responsible for a large fraction of the total PVA

411     diagnosed along both tropopause breaks, additional insight is found by partitioning the non-

412     divergent wind field via the piecewise PV inversion techniques described in Section 2. The non-

413     divergent wind and PVA associated with the MPV, UTPV, and IPV are each shown in Fig. 7.

414     The SPV non-divergent wind had a negligible influence on the diagnosed horizontal

415     displacement of the polar and subtropical tropopause breaks during this case and is not included

416     in the subsequent analysis. Figures 7a,b demonstrate that the MPV non-divergent wind was

417     characterized by a confluent flow pattern that accounted for a substantial fraction of the total

418     PVA that was diagnosed along both the polar and subtropical tropopause breaks in Figs. 6a,b.

419     The confluent flow pattern associated with the MPV also conforms well to the conceptual model

420     presented in Fig. 2 and appears to be essential for positioning the polar and subtropical

421     tropopause breaks in close proximity to one another.

422     The UTPV non-divergent wind was characterized by a broad cyclonic circulation that

423     was maximized in the immediate vicinity of the PV hook at 300 hPa (Figs. 7c,d). The UTPV

424     non-divergent wind was responsible for PVA along the polar tropopause break (Fig. 7c) that was

425     of similar magnitude to that forced by the MPV non-divergent wind, but opposite in sign. In

426     particular, the UTPV non-divergent wind was responsible for a strip of –PVA from northern

427     Mississippi to the Mid-Atlantic coast (Fig. 7c) that was collocated with a strip of +PVA by the

428     MPV non-divergent wind (Fig. 7a). Consequently, the competing influence of the UTPV and

429     MPV non-divergent wind resulted in the weak total PVA that was diagnosed along the portion of

430     the polar tropopause break that paralleled the subtropical tropopause break at this time (Fig. 6a).

431     While the MPV non-divergent wind (Fig. 7b) was responsible for a large fraction of the

432     total +PVA diagnosed along the subtropical tropopause break west of the Florida peninsula (Fig.

18

433    6b), the MPV (Fig. 7b) and UTPV (Fig. 7d) non-divergent wind combined constructively to

434    account for the total –PVA diagnosed east of Florida (Fig. 6b). Specifically, the UTPV non-

435    divergent wind was characterized by southerly flow along the East Coast that resulted in a strip

436    of –PVA east of South Carolina. As a result, both the UTPV and MPV non-divergent wind

437    influenced the diagnosed poleward displacement of the subtropical tropopause break over the

438    Atlantic Ocean (Fig. 6b) that favored a vertical alignment of the two tropopause breaks near that

439    location 18-h later.

440          Figures 7e,f demonstrate the IPV non-divergent flow was characterized by two

441    perturbation anticyclones, with one located east of New England and another situated over the

442    Gulf of Mexico. The perturbation anticyclone east of New England was a direct product of the

443    diabatic erosion of upper-tropospheric PV that accompanied the developing surface cyclone and

444    its extensive precipitation shield (Fig. 5). However, it is apparent at this time that the

445    perturbation anticyclone east of New England was positioned too far downstream to have an

446    influence on the lateral displacement of the polar and subtropical tropopause breaks over the

447    southeastern United States. In contrast, the perturbation anticyclone over the Gulf of Mexico was

448    more favorably located to displace the subtropical tropopause break (Fig. 7f) and was associated

449    with the outflow from persistent tropical convection downstream of the low-latitude trough

450    (WM16; their Figs. 6,8). Despite its favorable location, however, the IPV non-divergent wind

451    only accounted for weak –PVA along the subtropical tropopause break over Mexico (Fig. 7f) and

452    was strongly outweighed by the +PVA accomplished by the MPV non-divergent wind in that

453    same location (Fig. 7b).

454          The substantial influence of the UTPV non-divergent wind on the diagnosed horizontal

455    displacement of the tropopause breaks at this time motivates an examination of the non-divergent

456    wind associated with the PJPV and STJPV. Recall that the PJPV and STJPV are not a strict

457    partition of the UTPV, but their sum closely approximates the distribution of UTPV. The PJPV

458    non-divergent wind was characterized by a perturbation cyclone that was centered squarely on

459    the PV hook at 300 hPa (Fig. 8a). Furthermore, the non-divergent wind associated with the PJPV

460    was maximized on the southernmost edge of the PV hook at this time, coincident with the

461    location of the PJ axis in Fig. 5b. Figure 8a demonstrates that the PJPV non-divergent wind

462    contributed substantially to the PVA by the UTPV non-divergent wind diagnosed along the polar

463    tropopause break, as well, with PVA of the same sign and in the same locations as shown in Fig.

464    7c. The strength of the PJPV non-divergent wind was markedly weaker at 200 hPa, however, due

465    to the strong static stability residing above the isentropic layer used to isolate the PJPV (Fig. 4b).

466    Consequently, the PJPV non-divergent wind (Fig. 8b) only accounted for a small fraction of the

467    –PVA by the UTPV non-divergent wind diagnosed along the subtropical tropopause break in

468    Fig. 7d off the coast of South Carolina.

469        The STJPV non-divergent wind was maximized in the vicinity of the STJ axis along the

470    subtropical tropopause break (Figs. 8c,d) and bore a great deal of qualitative similarity to the

471    UTPV non-divergent wind pattern (Figs. 7c,d). At 300 hPa, the STJPV non-divergent wind was

472    associated with PVA patterns along the polar tropopause break (Fig. 8c) that were nearly

473    identical to those associated with the PJPV (Fig. 8a), which suggests that both the PJPV and

474    STJPV non-divergent wind had a comparable influence on the diagnosed lateral displacement of

475    the polar tropopause break by the UTPV non-divergent wind (Fig. 7c). However, Fig. 8d shows

476    that the STJPV non-divergent wind accounted for nearly all of the PVA by the UTPV non-

477    divergent wind along the subtropical tropopause break in Fig. 7d. As a result, it appears that the

478    non-divergent circulation associated with the STJPV had a greater ability to laterally displace

479    *both* the polar and subtropical tropopause breaks.

480    *c) Vertical Displacement of the Tropopause Breaks*

481    Thus far, the analysis suggests that jet superposition via differential horizontal

482    displacement of the two tropopause breaks was favored off the coast of South Carolina due to

483    contributions from the non-divergent wind associated with the MPV and UTPV, which includes

484    the PJPV and STJPV. Recall from the conceptual model in Fig. 3, however, that vertical motion

485    can also contribute to the production of a jet superposition. Consequently, the analysis must also

486    consider the vertical displacement of the tropopause accomplished by the balanced vertical

487    motion field. The balanced vertical motion field at 1800 UTC 19 December was characterized by

488    a strip of subsidence at 400 hPa that was positioned squarely between the polar and subtropical

489    tropopause breaks (Fig. 9a). Furthermore, a vertical cross section[5], C–C', through both

490    tropopause breaks indicates that the subsidence was positioned directly on and beneath the

491    subtropical tropopause step and polar tropopause break (Fig. 9b). This subsidence was

492    responsible for a band of +PVA along the tropopause that favored a downward displacement of

493    the tropopause and an erosion of the subtropical tropopause step, both of which would contribute

494    to jet superposition.

495    As for the non-divergent wind, the vertical motion can be partitioned by employing a

496    piecewise inversion of the prognostic balance equations. While the MPV non-divergent wind had

497    a substantial influence on horizontally displacing the polar and subtropical tropopause breaks,

498    Fig. 10a indicates that the MPV only accounted for a small fraction of the subsidence diagnosed

499    between the two tropopause breaks. In contrast, the UTPV was associated with a continuous

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[5] The subsidence diagnosed along the cross section, C–C', is representative of cross sections in all locations where the polar and subtropical tropopause breaks parallel one another over the southeastern United States and is chosen to match the cross section shown at this time by WM16.

500    band of subsidence that extended along the polar tropopause break from Kansas to the East Coast

501    (Fig. 10b), most of which was attributable to the PJPV (Fig. 10e) rather than the STJPV (Fig.

502    10f). The IPV (Fig. 10c) and SPV (Fig. 10d) were also associated with notable subsidence

503    between the two tropopause breaks, with most of the subsidence confined to the southeastern

504    United States and in the immediate vicinity of the surface cyclone. Consequently, the analysis in

505    Fig. 10 suggests that PV perturbations associated with the PJ, the surface cyclone, and the

506    surface cyclone's precipitation shield were most responsible for the production of subsidence

507    that would aid in the development of a jet superposition.

508         WM16 demonstrated a large fraction of the subsidence observed between the two jet

509    cores at this time was attributable to the ageostrophic transverse circulation associated with the

510    double jet structure (their Figs. 10c,d). An advantage afforded by the piecewise PV inversion

511    techniques employed in this study is the ability to partition the ageostrophic transverse

512    circulation diagnosed by WM16 and to identify the dynamical structures most responsible for its

513    production. The ageostrophic transverse circulation can be partitioned using the piecewise form

514    of the Sawyer–Eliassen circulation equation (Sawyer 1956; Eliassen 1962) proposed by Morgan

515    (1999):

516    $$\left(\gamma\frac{\partial\theta}{\partial p}\right)\frac{\partial^2\psi_{se}}{\partial y^2} + \left(2\frac{\partial M}{\partial p}\right)\frac{\partial^2\psi_{se}}{\partial y\partial p} + \left(-\frac{\partial M}{\partial y}\right)\frac{\partial^2\psi_{se}}{\partial p^2} = 2\gamma\left(\frac{\partial U_g'}{\partial y}\frac{\partial\theta}{\partial x} + \frac{\partial V_g'}{\partial y}\frac{\partial\theta}{\partial y}\right) \qquad (1)$$

517    where $\gamma$ is a constant on isobaric surfaces [ $\gamma = (R/fp_o)(p_o/p)^{c_v/c_p}$ ], $p_o$=1000 hPa, $c_v$=718 J

518    kg$^{-1}$ K$^{-1}$, $c_p$=1004 J kg$^{-1}$ K$^{-1}$, $R$ is the gas constant for dry air, $\theta$ is the potential temperature, and $f$

519    is the Coriolis parameter. $M$ is defined as the absolute geostrophic momentum and $U_g'$ and $V_g'$ are

520    the perturbation geostrophic wind components recovered from an inversion of a subset of the PV

521    distribution ( $\vec{V_g'} = \frac{1}{f}\,\hat{k}\times\nabla\phi'$ ). The ageostrophic transverse circulation lies in a vertical plane

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522     perpendicular to the jet axes and is determined by the Sawyer–Eliassen streamfunction, $\psi_{se}$, such

523     that the across-jet ageostrophic wind and vertical motion are defined as $v_{ag} = -\partial\psi_{se}/\partial p$ and

524     $\omega = dp/dt = \partial\psi_{se}/\partial y$, respectively.

525         The technique for partitioning the ageostrophic tranverse circulation consists of isolating

526     the geostrophic wind associated with each subset of the PV distribution and using those

527     components of the geostrophic wind to calculate the right hand side of (1). Solution to (1) then

528     proceeds by using the full distribution of $\theta$ and $M$ to calculate the coefficients on the left hand

529     side of (1) and by employing an identical method for inversion as outlined in WM16. Given that

530     all of the operators in (1) are linear, the ageostrophic transverse circulations associated with each

531     subset of the PV distribution add together to produce the full ageostrophic transverse circulation

532     forced by the total geostrophic wind. The reader is referred to Eliassen (1962) or Keyser and

533     Shapiro (1986) for a more detailed discussion of the Sawyer–Eliassen circulation equation and to

534     Morgan (1999) for a discussion on the piecewise form of the equation.

535         Figure 11a shows the ageostrophic transverse circulation within the cross section, C–C',

536     in Fig. 5b that was calculated using the total geostrophic wind from the full PV inversion.

537     Importantly, the circulation in Fig. 11a is nearly identical that shown in Fig. 10c of WM16,

538     which was computed using the geostrophic wind field from the GFS analysis. The ageostrophic

539     transverse circulation in Fig. 11a was responsible for a substantial fraction of the +PVA

540     diagnosed along the tropopause in Fig. 9b, as the subsidence driven by the ageostrophic

541     transverse circulation was favorably located on and beneath the subtropical tropopause step. A

542     partition of the ageostrophic transverse circulation into the piecewise circulations forced by the

543     MPV (Fig. 11b) and PPV (Fig. 11c) geostrophic wind demonstrates that a majority of the +PVA

544 and subsidence in Fig. 11a was associated with the ageostrophic transverse circulation tied to the

545 PPV.

546     The ageostrophic transverse circulation associated with the PPV can be further

547 partitioned into the individual circulations forced by the UTPV, IPV, and SPV geostrophic wind.

548 Figure 12 indicates that the largest fraction of the PPV's ageostrophic transverse circulation was

549 forced by the UTPV geostrophic wind (Fig. 12a), with minor and negligible contributions from

550 the transverse circulations forced by the IPV (Fig. 12b) and SPV (Fig. 12c) geostrophic wind,

551 respectively[6]. This result aligns well with the partition of the complete vertical motion field

552 shown in Fig. 10, which attributed the greatest amount of subsidence between the polar and

553 subtropical tropopause breaks to the UTPV in the vicinity of the cross section, C–C'. The UTPV

554 transverse circulation (Fig. 12a) can be further divided, approximately, into the ageostrophic

555 transverse circulations associated with the PJPV (Fig. 12d) and STJPV (Fig. 12e). Notably, a

556 comparison between Fig. 12d and Fig. 12e indicates that a greater fraction of the UTPV's

557 ageostrophic transverse circulation was associated with the PJPV. Consequently, the analysis

558 provides additional evidence indicating that the flow associated with the PJPV had a greater

559 ability to vertically restructure the tropopause than the flow associated with the STJPV.

560 **4. Discussion**

561     The preceding analysis provides additional support for the results in WM16 and for the

562 role that vertical motion, and particularly ageostrophic transverse circulations, played in the

563 production of a jet superposition during the 18–20 December 2009 Mid-Atlantic Blizzard. The

564 PV analysis also indicated that differential horizontal displacement of the polar and subtropical

565 tropopause breaks contributed substantially to the development of a jet superposition east of the

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[6] Vertical cross sections taken further downstream at this time show much more substantial contributions from the ageostrophic transverse circulations associated with the IPV and SPV, consistent with the analysis in Fig. 10.

566  Florida peninsula. These two processes are summarized succinctly in Fig. 13, which shows both

567  a systematic poleward displacement of the subtropical tropopause break and a steady downward

568  displacement of the subtropical tropopause step during the period 1800 UTC 19 December–1200

569  UTC 20 December. It is noteworthy to mention that, near the end of this 18-h period, the polar

570  tropopause break became characterized by weak total +PVA due the MPV non-divergent wind

571  (not shown). This result encouraged an equatorward displacement of the polar tropopause break

572  and contributed to the completion of jet superposition. Overall, both the movement of the

573  tropopause breaks and the downward displacement of the subtropical tropopause step shown in

574  Fig. 13 are completely in line with the conceptual model presented in Fig. 3.

575       The role played by vertical displacement in this case may not be representative of all

576  superposition cases, however, as it is possible that other cases may be solely characterized by a

577  differential horizontal displacement of the two tropopause breaks. Furthermore, additional cases

578  may be associated with proximate latent heat release that could act to erode PV in the vicinity of

579  the three-step tropopause structure in a manner that encourages jet superposition. Consequently,

580  a more comprehensive examination of superposition events is required to ascertain the mode

581  through which jet superpositions develop most frequently over North America.

582       A novel perspective provided by this analysis was the ability to partition the flow and to

583  attribute the development of a superposed jet to dynamical structures present throughout the

584  troposphere and lower stratosphere during the event. In particular, the MPV non-divergent wind

585  was characterized by a large-scale, confluent flow pattern over the eastern United States that

586  aligned well with the conceptual model presented in Fig. 2. This confluent flow pattern was

587  essential in transporting PV perturbations along both the polar and subtropical waveguides

588  towards middle latitudes where they could interact with one another to restructure the tropopause

589  and produce a superposition. Additional work is underway to examine whether the presence of a

590  large-scale, confluent flow pattern is a common element of jet superposition events over North

591  America and to evaluate the variability in upstream flow patterns that are conducive to jet

592  superpositions. The ability to identify large-scale flow patterns that favor the development of jet

593  superposition events could aid in identifying particular forecast periods that present an increased

594  likelihood for jet superpositions and, consequently, for the development of high-impact weather.

595  Aside from the role played by the MPV non-divergent wind, the three-dimensional

596  circulation associated with the UTPV accounted for the largest fraction of the total PVA

597  diagnosed along the tropopause at 1800 UTC 19 December. This result implies that PV

598  perturbations associated with the PJ and STJ had the greatest influence on restructuring the

599  tropopause during the event. While the IPV and SPV non-divergent wind did not impact the

600  horizontal displacement of the tropopause breaks, the IPV and SPV contributed to the subsidence

601  diagnosed between the two tropopause breaks. Consequently, the surface cyclone off the East

602  Coast, and its associated diabatic heating, played a less substantial, though important role in the

603  development of the superposition.

604  It is possible, however, that the SPV and IPV may play a larger role in restructuring the

605  tropopause during superposition cases with more intense cyclogenesis and proximate latent heat

606  release. Furthermore, the influence of the divergent wind was found to be minimal during the

607  18–20 December 2009 Blizzard. However, WM16 demonstrated that cases with extensive

608  midlatitude convection in the vicinity of a double jet structure, such as the 1–3 May 2010

609  Nashville Flood, can be characterized by much stronger horizontal displacement of the

610  tropopause by the upper-tropospheric divergent wind. Consequently, a greater sampling of jet

611    superposition events is required to describe the characteristic types of interactions between PV

612    perturbations during jet superposition events.

613         The substantial role played by the three-dimensional circulation associated with the

614    UTPV in this case motivated isolating the influence of PV perturbations associated with the PJ

615    and STJ. Interestingly, the analysis demonstrated that the STJPV non-divergent wind had a

616    stronger ability to *horizontally* restructure the tropopause than the PJPV non-divergent wind.

617    Physically, the PJPV non-divergent wind was limited in its ability to displace the subtropical

618    tropopause break because of the strong static stability residing above the isentropic layer used to

619    isolate PV perturbations associated with the PJ (Fig. 4). Consequently, the penetration depth of

620    the PJPV's non-divergent circulation above the polar tropopause break was extremely shallow.

621    In contrast, the STJPV's non-divergent circulation was characterized by a deeper penetration

622    depth below the isentropic layer used to isolate PV perturbations associated with the STJ, given

623    the weaker static stability of the upper troposphere. This contrast in the vertical extent of the

624    non-divergent circulations associated with the PJPV and STJPV permitted the STJPV non-

625    divergent wind to have a stronger influence on horizontally displacing both tropopause breaks.

626         An examination of the vertical motion associated with the PJPV and STJPV indicated

627    that the three-dimensional circulation associated with the PJPV had a stronger ability to

628    *vertically* restructure the tropopause. Some insight into the difference between the vertical

629    motion field associated with the PJPV and STJPV is found by considering the forcing terms on

630    the right hand side of the Sawyer–Eliassen circulation equation. Given that stronger baroclinicity

631    typically resides beneath the PJ, the PJPV geostrophic wind is maximized in the immediate

632    vicinity of the strongest tropospheric baroclinicity, by definition. In contrast, the STJPV's

633    horizontal geostrophic circulation has to penetrate downward and laterally before it can interact

634　with the strongest baroclinicity. Consequently, the PJPV geostrophic wind forces a stronger

635　response from the Sawyer–Eliassen circulation equation than the STJPV geostrophic wind and,

636　correspondingly, more intense subsidence beneath the subtropical tropopause step. The results

637　from this case imply broadly that PV perturbations associated with the PJ and STJ may have

638　distinctly different roles with respect to their ability to restructure the tropopause. However,

639　additional evidence is required to verify this suggestion.

640　　　　Finally, the techniques employed within this study offer a novel perspective from which

641　to examine a number of different tropospheric phenomena. For example, the jet PV partition can

642　be employed to further corroborate the results of Martius et al. (2010), who found that wave

643　activity can be transferred from one waveguide to another, and to more broadly examine the

644　nature of the interaction between the polar and subtropical waveguides. The jet PV partition also

645　holds promise in its ability to interrogate a number of different phenomena that may occur within

646　an environment characterized by multiple jet structures, such as surface cyclogenesis and

647　extratropical transition. Lastly, the piecewise inversion of the Sawyer–Eliassen circulation

648　equation employed in this study has the potential to provide richer detail into the nature of

649　transverse frontal circulations.

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810          rivers. *Mon. Wea. Rev.*, **126,** 725–735.

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812

813  **Figure Captions**

814  FIG. 1. (a) Vertical cross section, A–A', in Fig. 5a through separate polar and subtropical jet

815  cores at 0000 UTC 19 December 2009, with potential temperature contoured in red every 5-K,

816  wind speed shaded following the legend in m s$^{-1}$, and the 2-PVU surface contoured with the

817  thick blue line. 'PJ' and 'STJ' identify a polar and subtropical jet core, respectively, and the

818  individual tropopause steps are labeled accordingly. (b) As in (a), but for the vertical cross

819  section, B–B' in Fig. 5c, through a superposed jet at 1200 UTC 20 December 2009.

820

821  FIG. 2. Conceptual diagram summarizing the development of a jet superposition. The orange

822  arrows depict the branches of an ageostrophic transverse circulation, the green circle identifies an

823  area of convection, and the + (–) symbol corresponds to the center of a polar cyclonic (tropical

824  anticyclonic) PV perturbation, with the blue (red) arrow indicating the movement that particular

825  perturbation towards middle latitudes. The purple fill pattern corresponds to isotachs, with the

826  darker shade of purple identifying faster wind speeds. The locations of the polar jet ('PJ'),

827  subtropical jet ('STJ'), and superposed jets are labeled accordingly. For additional information

828  on interpretation, please refer to the discussion in the text.

829

830  FIG. 3. Conceptual diagram illustrating the two ways a three-step tropopause can be restructured

831  into the two-step tropopause characteristic of a superposed jet. The thick black line corresponds

832  to the 2-PVU surface within the cross section, A–A', in Fig. 5a, with the gray shading identifying

833  the stratosphere. The red arrows correspond to the horizontal displacement of an individual

834  tropopause break and the blue arrows identify a vertical displacement of the subtropical

835  tropopause step.

836

837    FIG. 4. (a) Conceptual schematic of the three-way partitioning scheme for the Perturbation PV

838    overlaid on top of the cross section, A–A', in Fig. 5a. Potential temperature is contoured in red

839    every 5-K, the 2-PVU surface is contoured with the thick black line, and the gray shading

840    identifies the stratosphere. Each box in the cross section corresponds to a subset of the PV

841    distribution and is drawn such that the top and bottom boundaries of the box identify the isobaric

842    layer used to isolate that subset of the PV distribution. The relative humidity (RH) criterion also

843    used to isolate each subset of the PV distribution is provided within each box. (b) Similar

844    conventions as in (a) but for the jet PV partitioning scheme. The + and – symbols correspond to

845    positive and negative PV perturbations, respectively, and the locations of the polar ('PJ') and

846    subtropical ('STJ') jets are labeled accordingly. The blue (red) shading identifies the isentropic

847    layer used to isolate the Polar Jet PV (Subtropical Jet PV). (c) Similar conventions as in (b) but

848    with the distribution of Subtropical Jet PV (Polar Jet PV) at 0000 UTC 19 December 2009

849    contoured every 1 PVU in yellow (light blue). Positive (negative) perturbation PV values are

850    denoted by the solid (dashed) contours.

851

852    FIG. 5. 250-hPa wind speed is shaded according to the legend in m s$^{-1}$, 250-hPa geopotential

853    height is contoured in black every 12 dam, sea level pressure is contoured in green every 4 hPa

854    below 1000 hPa, the location of the surface cyclone is identified with the red 'L', the

855    precipitation shield associated with the surface cyclone is shaded in green, and the jet axes are

856    identified according to the legend at (a) 0000 UTC 19 December 2009, (b) 1800 UTC 19

857    December 2009, and (c) 1200 UTC 20 December 2009.

858

859  FIG. 6. PV advection at 1800 UTC 19 December 2009 within the 1.5–2.5-PVU channel by the

860  non-divergent wind is shaded following the legend in $10^{-5}$ PVU s$^{-1}$ at (a) 300 hPa and (b) 200

861  hPa, with the non-divergent streamfunction contoured in black every $120\times10^5$ m$^2$ s$^{-1}$. PV

862  advection within the 1.5–2.5-PVU channel by the divergent wind is shaded as in (a,b) at (c) 300

863  hPa and (d) 200 hPa, with the divergent wind in excess of 5 m s$^{-1}$ plotted with vectors. The 2-

864  PVU surface at 300 hPa (200 hPa) is contoured in all panels with the blue (red) line and

865  corresponds to the location of the polar (subtropical) tropopause break.

866

867  FIG. 7. PV advection at 1800 UTC 19 December 2009 within the 1.5–2.5-PVU channel by the

868  non-divergent wind associated with the (a,b) Mean PV, (c,d) Upper-Tropospheric PV, and (e,f)

869  Interior PV at 300 hPa and 200 hPa, respectively. Conventions are identical to those in Fig. 6,

870  except with the streamfunction now contoured in black (negative values dashed) every $120\times10^5$

871  m$^2$ s$^{-1}$ in (a,b) and every $60\times10^5$ m$^2$ s$^{-1}$ in (c–f). The red 'L's (blue 'H's) correspond to local

872  minima (maxima) in streamfunction.

873

874  FIG. 8. PV advection at 1800 UTC 19 December 2009 within the 1.5–2.5-PVU channel by the

875  non-divergent wind associated with the (a,b) Polar Jet PV and (c,d) Subtropical Jet PV at 300

876  hPa and 200 hPa, respectively. Conventions are identical to those in Fig. 6, except with the

877  streamfunction now contoured in black (negative values dashed) every $30\times10^5$ m$^2$ s$^{-1}$. The red

878  'L's (blue 'H's) correspond to local minima (maxima) in streamfunction.

879

880  FIG. 9. (a) 400-hPa balanced vertical motion shaded according to the legend in dPa s$^{-1}$ at 1800

881  UTC 19 December 2009. The 2-PVU surface at 300 hPa (200 hPa) is contoured with the blue

882    (red) line and corresponds to the polar (subtropical) tropopause break. (b) Vertical cross section,

883    C–C', in (a), with potential temperature contoured in red every 5-K, wind speeds shaded

884    according to the legend in m s$^{-1}$, subsidence shaded according the legend in dPa s$^{-1}$, the 1.5-PVU

885    surface contoured with the blue line, and PV advection within the 1.5–2.5-PVU channel

886    accomplished by the sum of the vertical motion and horizontal divergent wind fields contoured

887    in yellow (negative values dashed) every $1\times10^{-5}$ PVU s$^{-1}$.

888

889    FIG. 10. 400-hPa balanced vertical motion associated with the (a) Mean PV, (b) Upper-

890    Tropospheric PV, (c) Interior PV, (d) Surface PV, (e) Polar Jet PV, and (f) Subtropical Jet PV at

891    1800 UTC 19 December 2009. Conventions are identical to those in Fig 9a.

892

893    FIG. 11. Vertical cross section, C–C', in Fig. 5b of the Sawyer–Eliassen streamfunction at 1800

894    UTC 19 December 2009 associated with the (a) Full PV, (b) Mean PV, and (c) Perturbation PV,

895    contoured in black (negative values dashed) every 300 m hPa s$^{-1}$, potential temperature

896    contoured in red every 5-K, wind speed shaded according to the legend in m s$^{-1}$, the 1.5-PVU

897    surface contoured in blue, subsidence associated with the Sawyer–Eliassen circulation shaded

898    according to the legend, and PV advection within the 1.5–2.5-PVU channel by the Sawyer–

899    Eliassen circulation contoured in yellow (negative values dashed) every $1\times10^{-5}$ PVU s$^{-1}$. The

900    arrowheads plotted on the streamfunction contours indicate the sense of the Sawyer–Eliassen

901    circulation.

902

903    FIG. 12. Vertical cross section, C–C', in Fig. 5b of the Sawyer–Eliassen streamfunction at 1800

904    UTC 19 December 2009 associated with the (a) Upper-Tropospheric PV, (b) Interior PV, (c)

905      Surface PV, (d) Polar Jet PV, and (e) Subtropical Jet PV, contoured in black (negative values

906      dashed) every 100 m hPa $s^{-1}$. All other conventions are identical to those in Fig. 11, except that

907      PV advection is now contoured in yellow (negative values dashed) every $0.5\times10^{-5}$ PVU $s^{-1}$.

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909      FIG. 13. Evolution of the 2-PVU surface within the cross section, B–B', in Fig. 5c during the

910      period 1800 UTC 19 December 2009–1200 UTC 20 December 2009.

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**Figures**

**FIG. 1.** (a) Vertical cross section, A–A', in Fig. 5a through separate polar and subtropical jet cores at 0000 UTC 19 December 2009, with potential temperature contoured in red every 5-K, wind speed shaded following the legend in m s$^{-1}$, and the 2-PVU surface contoured with the thick blue line. 'PJ' and 'STJ' identify a polar and subtropical jet core, respectively, and the individual tropopause steps are labeled accordingly. (b) As in (a), but for the vertical cross section, B–B' in Fig. 5c, through a superposed jet at 1200 UTC 20 December 2009.

**FIG. 2.** Conceptual diagram summarizing the development of a jet superposition. The orange arrows depict the branches of an ageostrophic transverse circulation, the green circle identifies an area of convection, and the + (–) symbol corresponds to the center of a polar cyclonic (tropical anticyclonic) PV perturbation, with the blue (red) arrow indicating the movement that particular perturbation towards middle latitudes. The purple fill pattern corresponds to isotachs, with the darker shade of purple identifying faster wind speeds. The locations of the polar jet ('PJ'), subtropical jet ('STJ'), and superposed jets are labeled accordingly. For additional information on interpretation, please refer to the discussion in the text.

**FIG. 3.** Conceptual diagram illustrating the two ways a three-step tropopause can be restructured into the two-step tropopause characteristic of a superposed jet. The thick black line corresponds to the 2-PVU surface within the cross section, A–A', in Fig. 5a, with the gray shading identifying the stratosphere. The red arrows correspond to the horizontal displacement of an individual tropopause break and the blue arrows identify a vertical displacement of the subtropical tropopause step.

**FIG. 4.** (a) Conceptual schematic of the three-way partitioning scheme for the Perturbation PV overlaid on top of the cross section, A–A', in Fig. 5a. Potential temperature is contoured in red every 5-K, the 2-PVU surface is contoured with the thick black line, and the gray shading identifies the stratosphere. Each box in the cross section corresponds to a subset of the PV distribution and is drawn such that the top and bottom boundaries of the box identify the isobaric layer used to isolate that subset of the PV distribution. The relative humidity (RH) criterion also used to isolate each subset of the PV distribution is provided within each box. (b) Similar conventions as in (a) but for the jet PV partitioning scheme. The + and – symbols correspond to positive and negative PV perturbations, respectively, and the locations of the polar ('PJ') and subtropical ('STJ') jets are labeled accordingly. The blue (red) shading identifies the isentropic layer used to isolate the Polar Jet PV (Subtropical Jet PV). (c) Similar conventions as in (b) but with the distribution of Subtropical Jet PV (Polar Jet PV) at 0000 UTC 19 December 2009 contoured every 1 PVU in yellow (light blue). Positive (negative) perturbation PV values are denoted by the solid (dashed) contours.
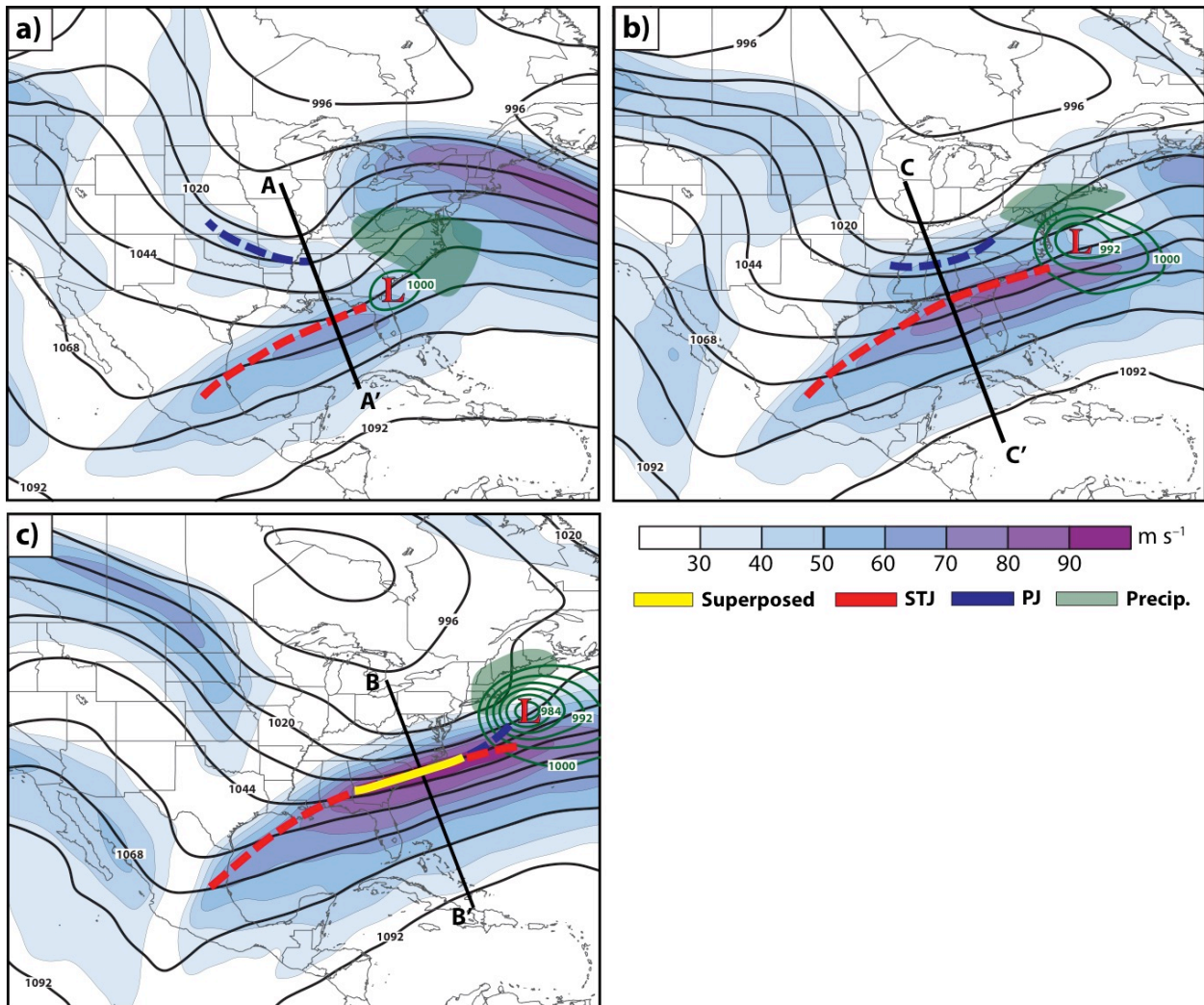
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**FIG. 5.** 250-hPa wind speed is shaded according to the legend in m s$^{-1}$, 250-hPa geopotential
height is contoured in black every 12 dam, sea level pressure is contoured in green every 4 hPa
below 1000 hPa, the location of the surface cyclone is identified with the red 'L', the
precipitation shield associated with the surface cyclone is shaded in green, and the jet axes are
identified according to the legend at (a) 0000 UTC 19 December 2009, (b) 1800 UTC 19
December 2009, and (c) 1200 UTC 20 December 2009.

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**300 hPa**

**200 hPa**

**Non-Divergent Wind**

**Divergent Wind**

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1041  **FIG. 6.** PV advection at 1800 UTC 19 December 2009 within the 1.5–2.5-PVU channel by the
1042  non-divergent wind is shaded following the legend in $10^{-5}$ PVU s$^{-1}$ at (a) 300 hPa and (b) 200
1043  hPa, with the non-divergent streamfunction contoured in black every $120 \times 10^5$ m$^2$ s$^{-1}$. PV
1044  advection within the 1.5–2.5-PVU channel by the divergent wind is shaded as in (a,b) at (c) 300
1045  hPa and (d) 200 hPa, with the divergent wind in excess of 5 m s$^{-1}$ plotted with vectors. The 2-
1046  PVU surface at 300 hPa (200 hPa) is contoured in all panels with the blue (red) line and
1047  corresponds to the location of the polar (subtropical) tropopause break.
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**FIG. 7.** PV advection at 1800 UTC 19 December 2009 within the 1.5–2.5-PVU channel by the non-divergent wind associated with the (a,b) Mean PV, (c,d) Upper-Tropospheric PV, and (e,f) Interior PV at 300 hPa and 200 hPa, respectively. Conventions are identical to those in Fig. 6, except with the streamfunction now contoured in black (negative values dashed) every $120\times10^5$ m$^2$ s$^{-1}$ in (a,b) and every $60\times10^5$ m$^2$ s$^{-1}$ in (c–f). The red 'L's (blue 'H's) correspond to local minima (maxima) in streamfunction.

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**FIG. 8.** PV advection at 1800 UTC 19 December 2009 within the 1.5–2.5-PVU channel by the non-divergent wind associated with the (a,b) Polar Jet PV and (c,d) Subtropical Jet PV at 300 hPa and 200 hPa, respectively. Conventions are identical to those in Fig. 6, except with the streamfunction now contoured in black (negative values dashed) every $30 \times 10^5$ m$^2$ s$^{-1}$. The red 'L's (blue 'H's) correspond to local minima (maxima) in streamfunction.
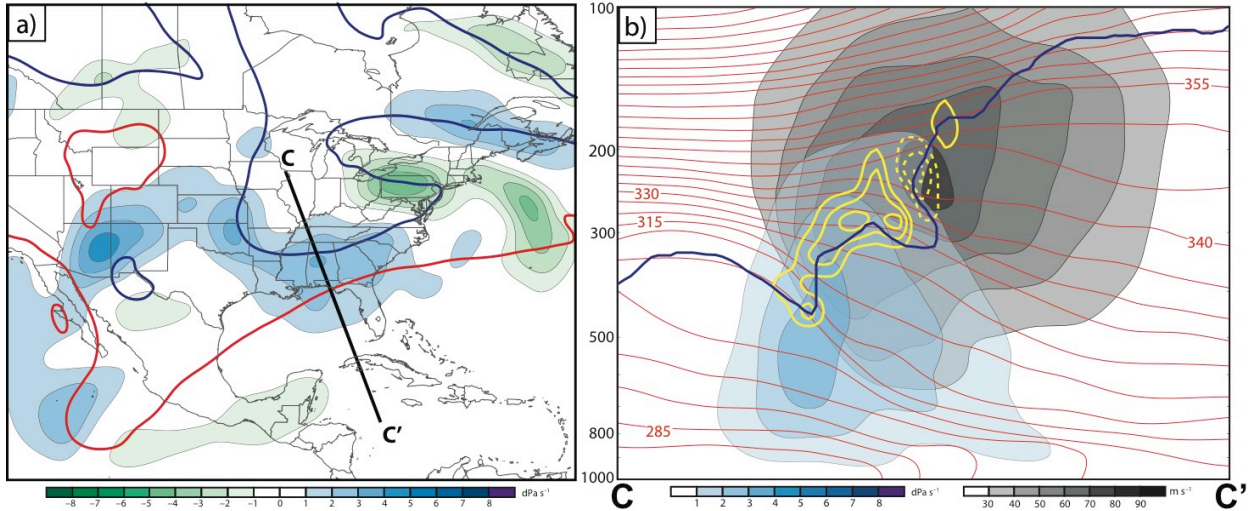
**FIG. 9.** (a) 400-hPa balanced vertical motion shaded according to the legend in dPa s$^{-1}$ at 1800 UTC 19 December 2009. The 2-PVU surface at 300 hPa (200 hPa) is contoured with the blue (red) line and corresponds to the polar (subtropical) tropopause break. (b) Vertical cross section, C–C', in (a), with potential temperature contoured in red every 5-K, wind speeds shaded according to the legend in m s$^{-1}$, subsidence shaded according the legend in dPa s$^{-1}$, the 1.5-PVU surface contoured with the blue line, and PV advection within the 1.5–2.5-PVU channel accomplished by the sum of the vertical motion and horizontal divergent wind fields contoured in yellow (negative values dashed) every $1\times10^{-5}$ PVU s$^{-1}$.
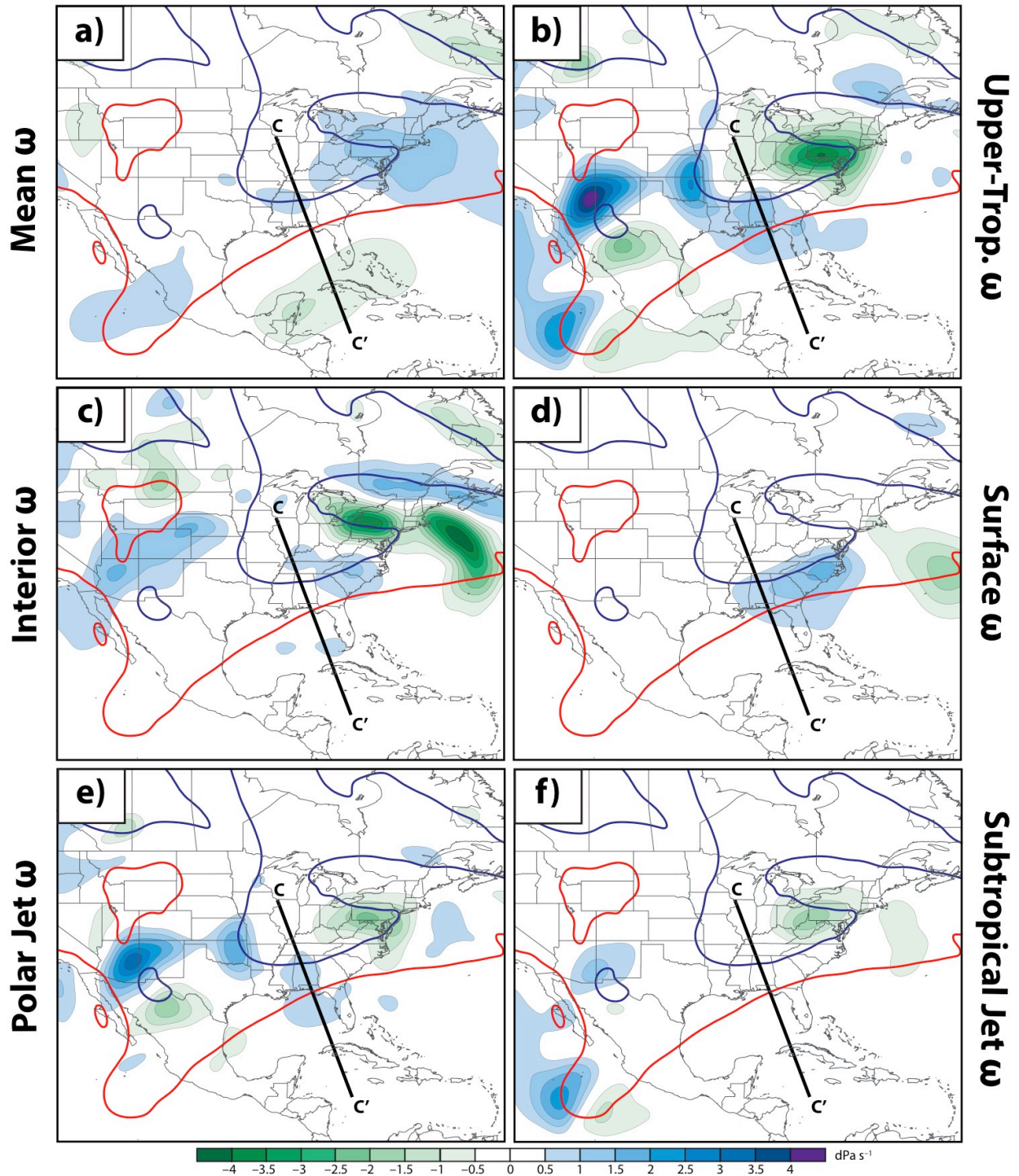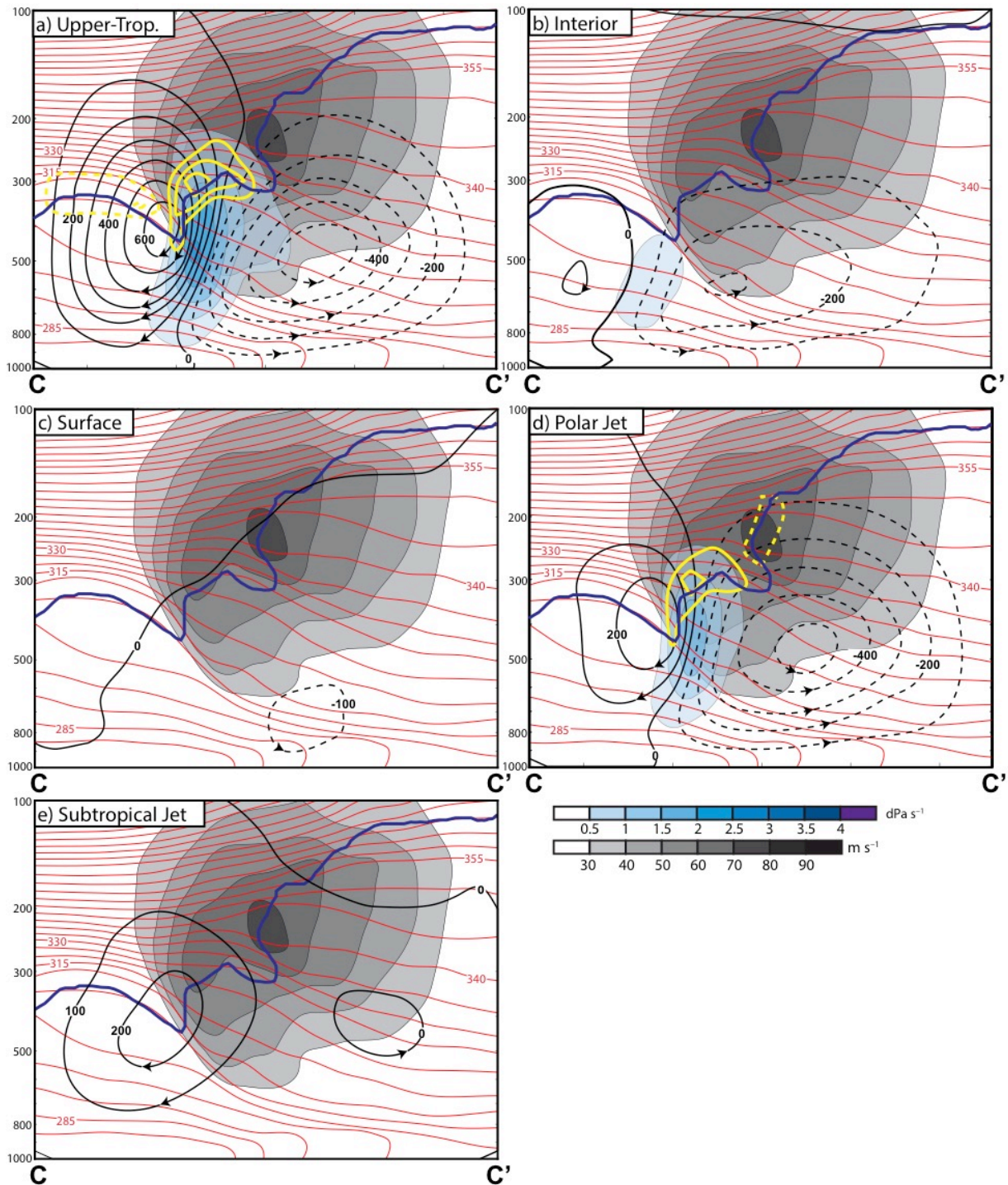
**FIG. 10.** 400-hPa balanced vertical motion associated with the (a) Mean PV, (b) Upper-Tropospheric PV, (c) Interior PV, (d) Surface PV, (e) Polar Jet PV, and (f) Subtropical Jet PV at 1800 UTC 19 December 2009. Conventions are identical to those in Fig 9a.

**FIG. 11.** Vertical cross section, C–C', in Fig. 5b of the Sawyer–Eliassen streamfunction at 1800 UTC 19 December 2009 associated with the (a) Full PV, (b) Mean PV, and (c) Perturbation PV, contoured in black (negative values dashed) every 300 m hPa s$^{-1}$, potential temperature contoured in red every 5-K, wind speed shaded according to the legend in m s$^{-1}$, the 1.5-PVU surface contoured in blue, subsidence associated with the Sawyer–Eliassen circulation shaded according to the legend, and PV advection within the 1.5–2.5-PVU channel by the Sawyer–Eliassen circulation contoured in yellow (negative values dashed) every $1\times10^{-5}$ PVU s$^{-1}$. The arrowheads plotted on the streamfunction contours indicate the sense of the Sawyer–Eliassen circulation.

1138 **FIG. 12.** Vertical cross section, C–C', in Fig. 5b of the Sawyer–Eliassen streamfunction at 1800
1139 UTC 19 December 2009 associated with the (a) Upper-Tropospheric PV, (b) Interior PV, (c)
1140 Surface PV, (d) Polar Jet PV, and (e) Subtropical Jet PV, contoured in black (negative values
1141 dashed) every 100 m hPa s$^{-1}$. All other conventions are identical to those in Fig. 11, except that
1142 PV advection is now contoured in yellow (negative values dashed) every $0.5 \times 10^{-5}$ PVU s$^{-1}$.
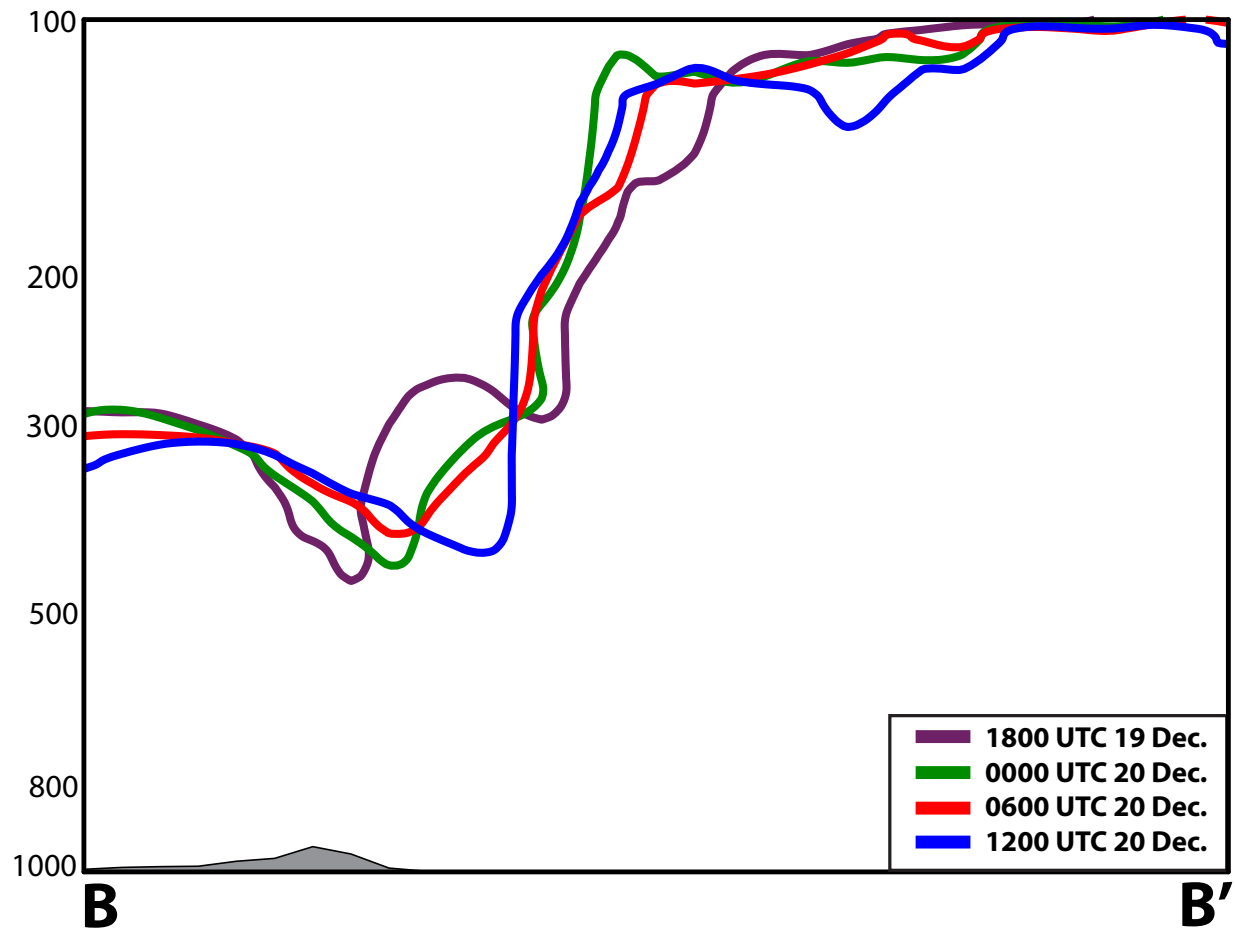
**FIG. 13.** Evolution of the 2-PVU surface within the cross section, B–B', in Fig. 5c during the period 1800 UTC 19 December 2009–1200 UTC 20 December 2009.